

# Data-Driven of Spatio-temporal Prediction: Earthquakes Case

**Group :** 14 (HZL) – Dataset 1

**Members :** Zhang Yumeng      Luo Wenjun      Huang Yi

**Instructors:** Prof. Gianmarco Mengaldo & Dr. Adriano Gualandi

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10/04/2023 presentation for 6 mins

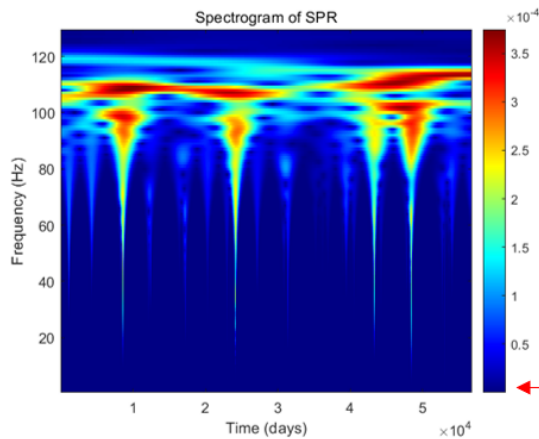
# CONTENT

- 1 System Analysis**
- 2 Order Reduction & Prediction**
- 3 Dynamic Mode Decomposition (DMD)**
- 4 Summary**

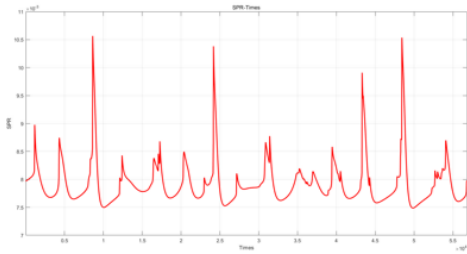


➤ System is dynamic spatio-temporal.

Temporal Analysis

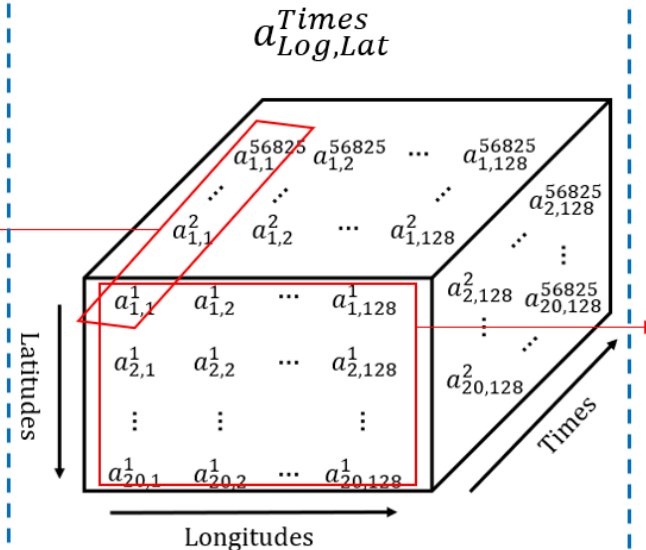


SPR Spectrogram

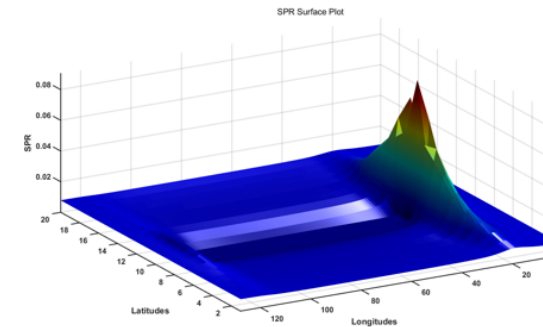


SPR Time Domain

Spatio-temporal Dataset



Spatio Analysis



SPR Surface



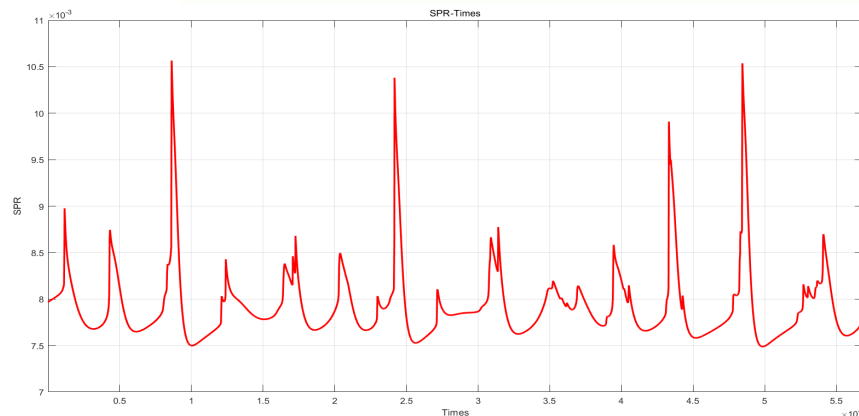
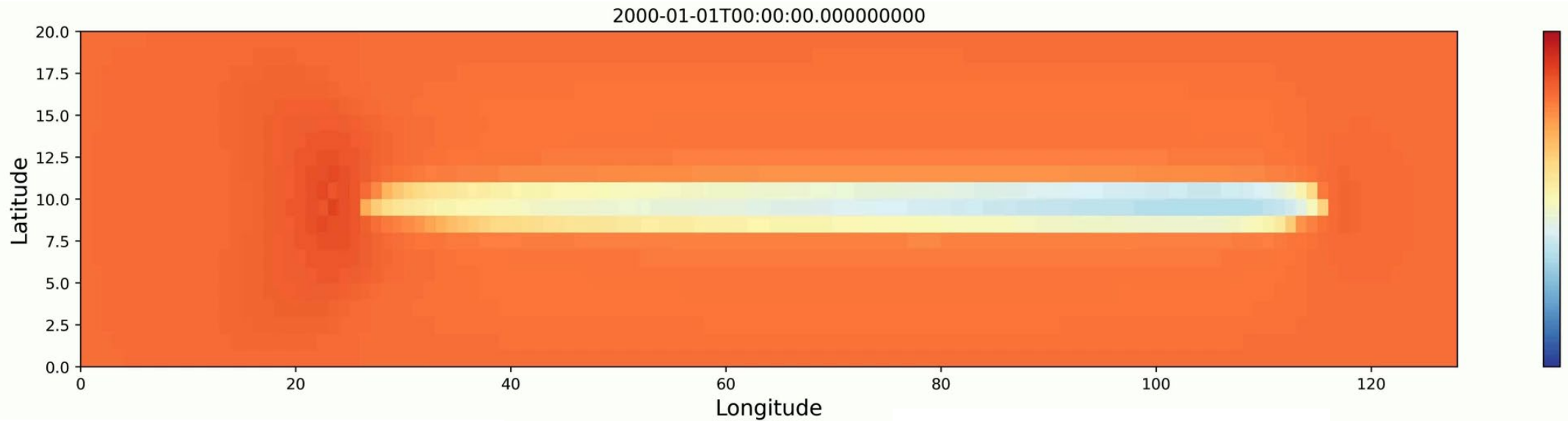
SPR Heatmap

## Conclusions

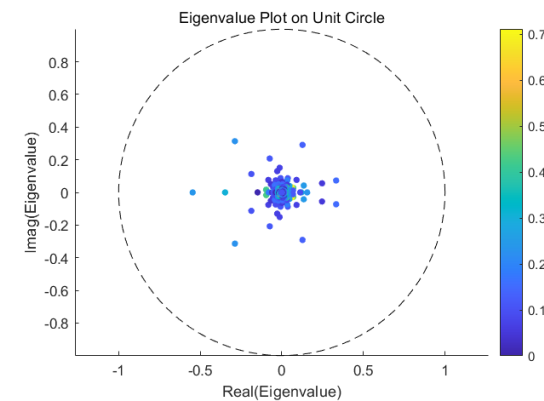
- Three dimensions.
- Spatial peaks exist.
- Variation with time periods.
- Energy concentration at 80-120Hz

➤ System is predictable.

Dataset  
Visualization



- A point in space has periodicity in the time dimension.



- The system is non-chaotic and decaying.





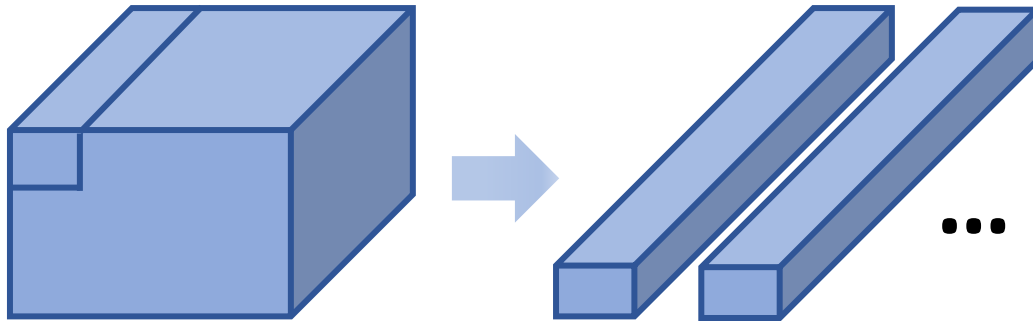
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# Time Series Prediction

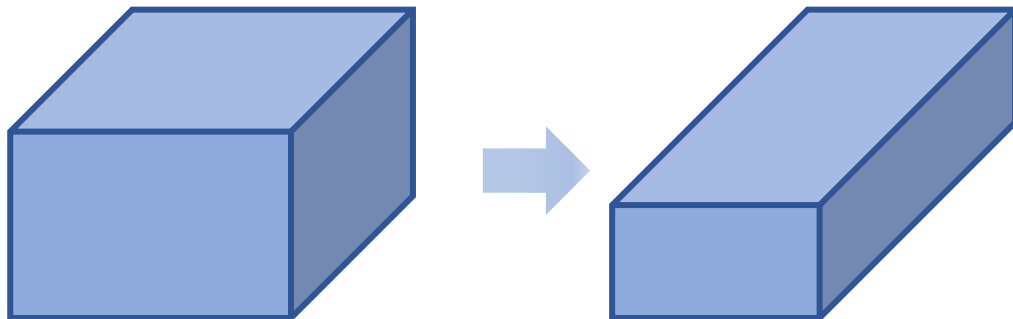
- Two prediction strategies for high-dimensional system.

## System segment



- Divide the system into a series of small subsystems to improve prediction accuracy.

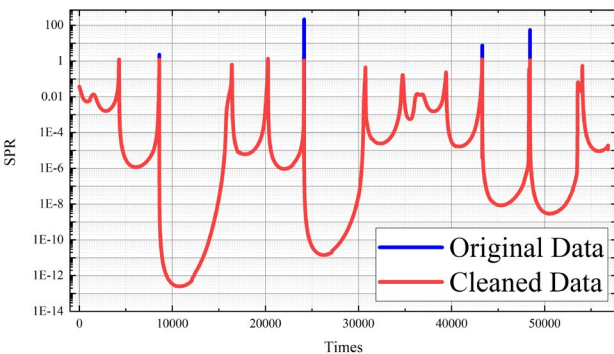
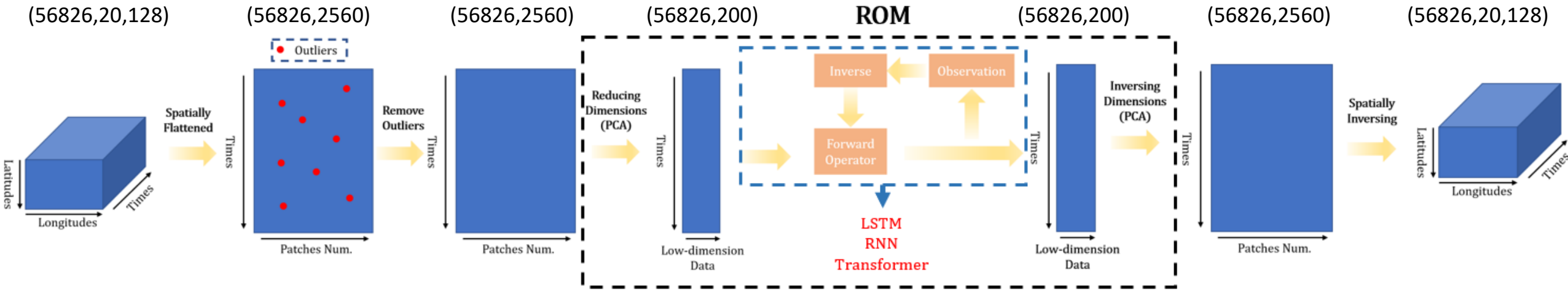
## Reduce system order



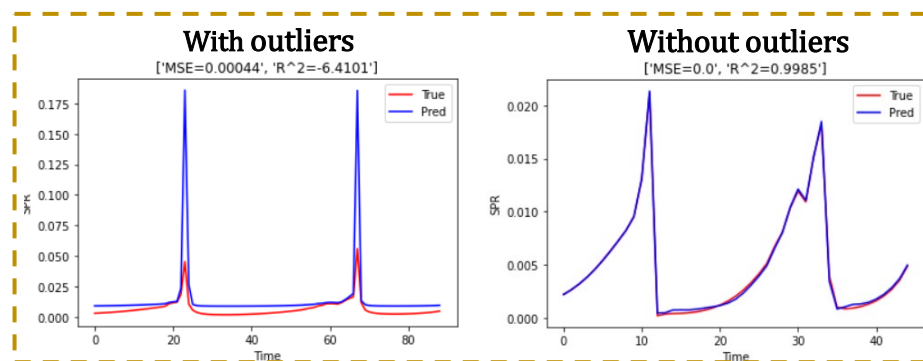
- Reduce the dimensions of system in space to reduce system complexity and computation.

# Reduced Order Model (ROM)

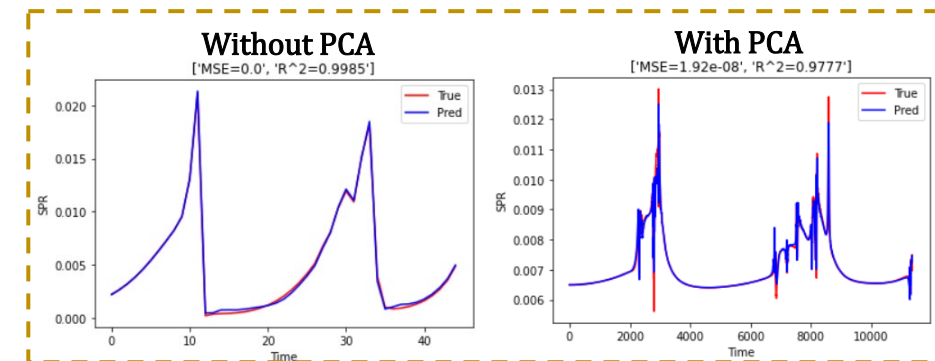
➤ Two prediction strategies for high-dimensional system.



Data comparison of preprocessing



Pred. comparison of with/without outliers



Pred. comparison of with/without PCA

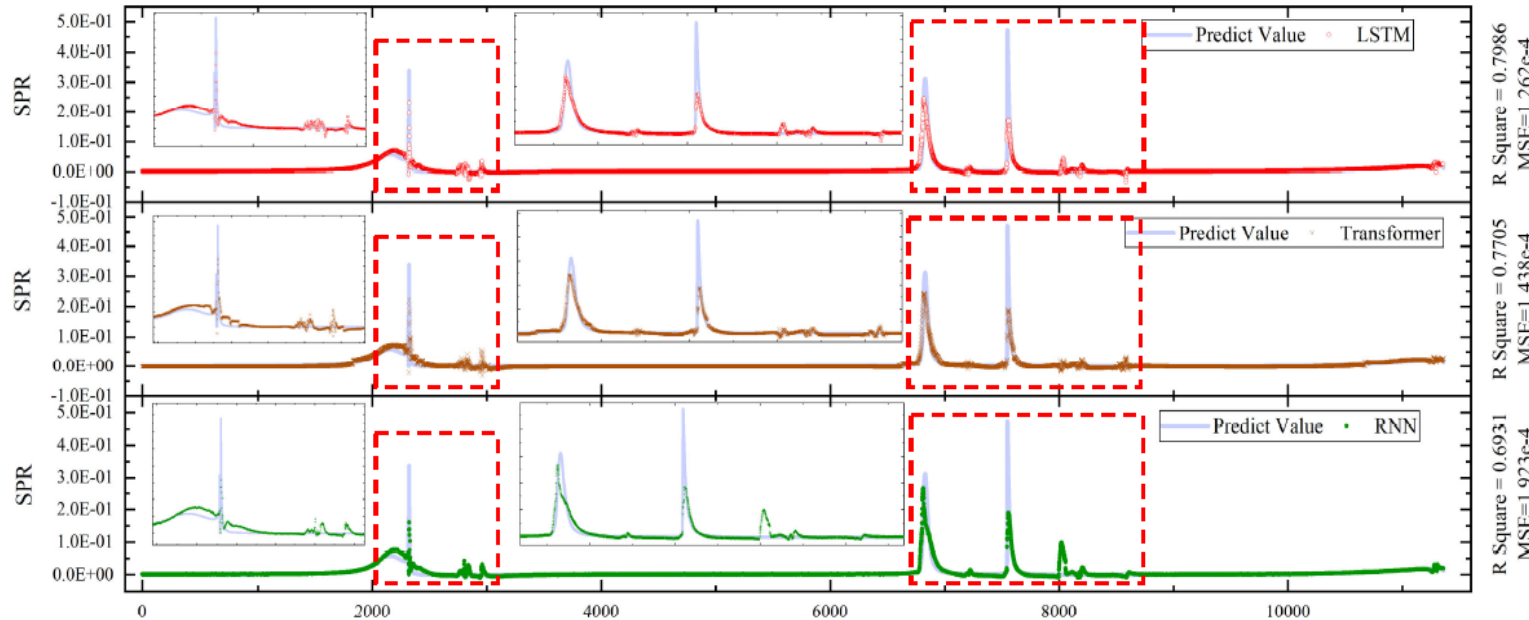
# Reduced Order Model (ROM)

## ➤ Prediction using LSTM with PCA and preprocessing.

LSTM

Transformer

RNN



### Seen in SPR-Time fig:

- LSTM has best performance among RNN and Transformer.
- All of them cannot fit well in peak region.

Name	R Square	MSE	Note
LSTM –With outliers – Without PCA	0.0183	0.0646	
<b>LSTM –Without outliers – Without PCA</b>	<b>0.9819</b>	<b>1.104e-5</b>	
LSTM – Without outliers – With PCA	0.8268	4.906e-5	Time: 199.27 s
LSTM – Without outliers – Without PCA	<b>0.9819</b>	<b>1.104e-5</b>	Time: 11873.31 s
<b>LSTM – Without outliers – With PCA</b>	<b>0.8268</b>	<b>4.906e-5</b>	
RNN – Without outliers – With PCA	0.4108	0.63143	
Transformer – Without outliers – With PCA	0.7989	6.750e-5	

### Summary:

- LSTM with PCA predicts well, has fast response and short training cost.
- PCA-based reduction loses a lot of system information.



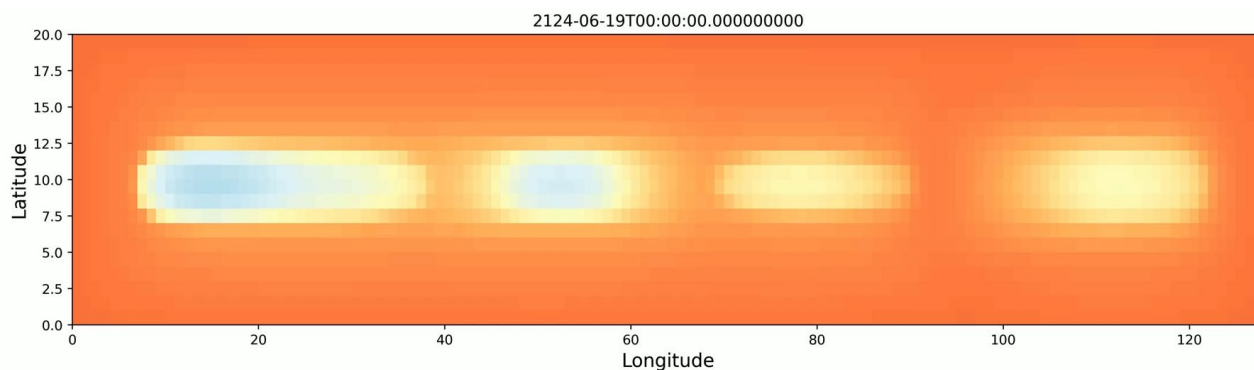
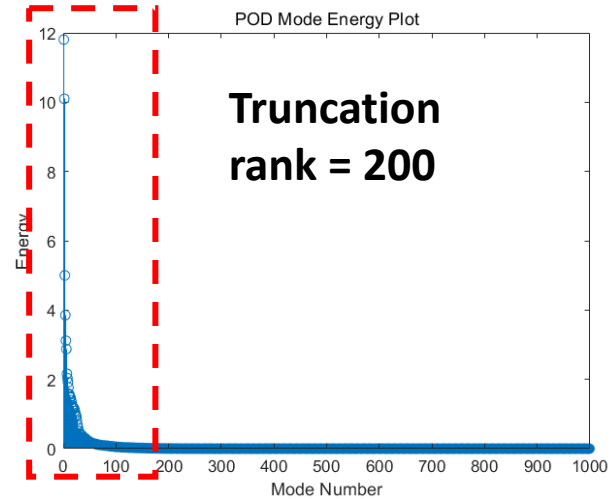
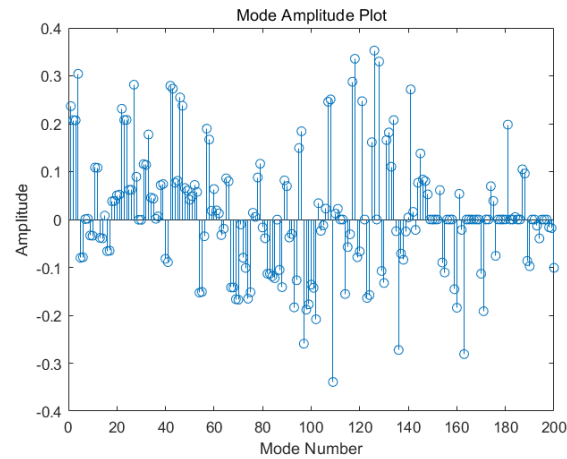
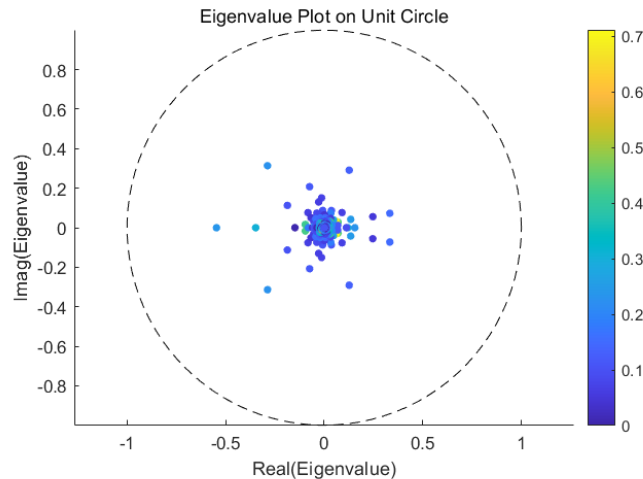


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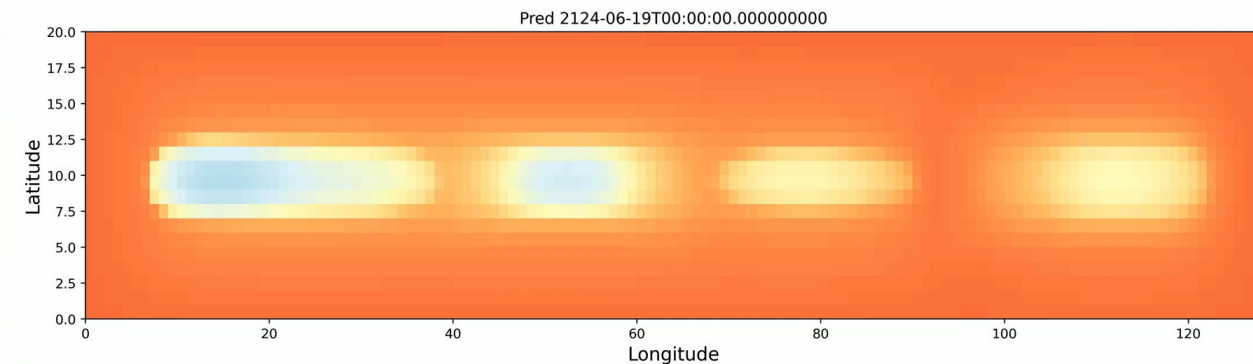
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# Dynamic Mode Decomposition (DMD)

## ➤ Prediction using DMD - Koopman.



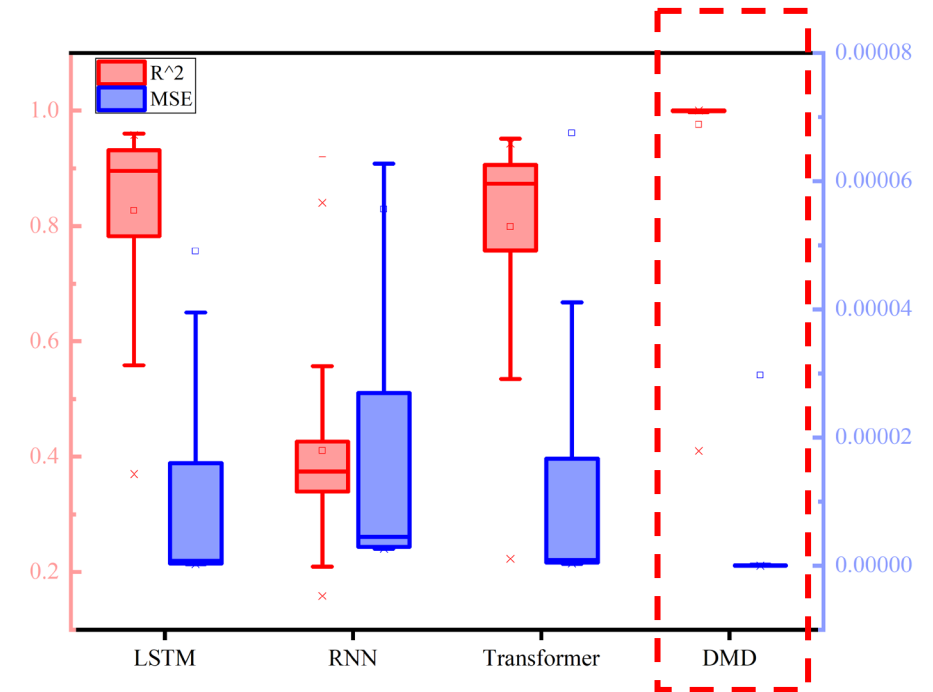
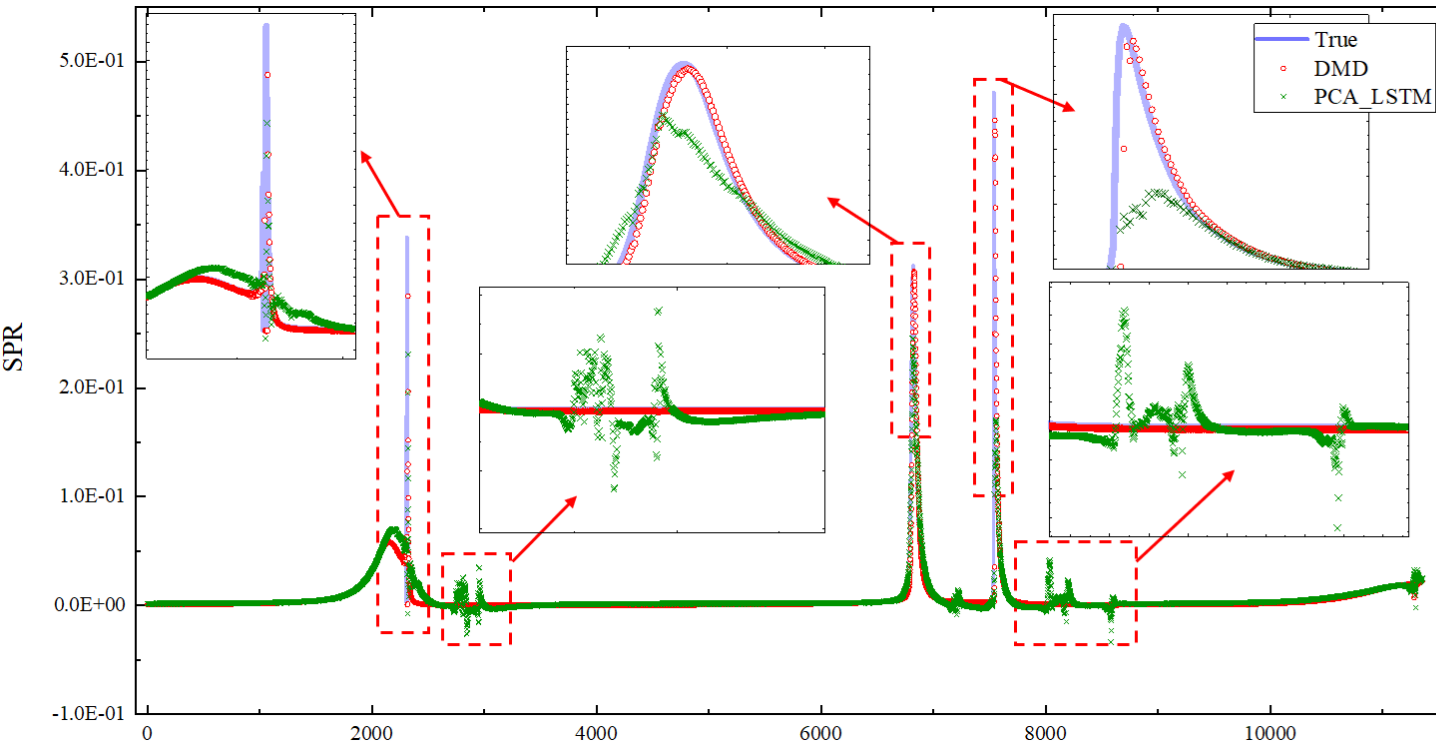
True



DMD Pred

# Dynamic Mode Decomposition (DMD)

## ➤ Prediction using DMD - Koopman.



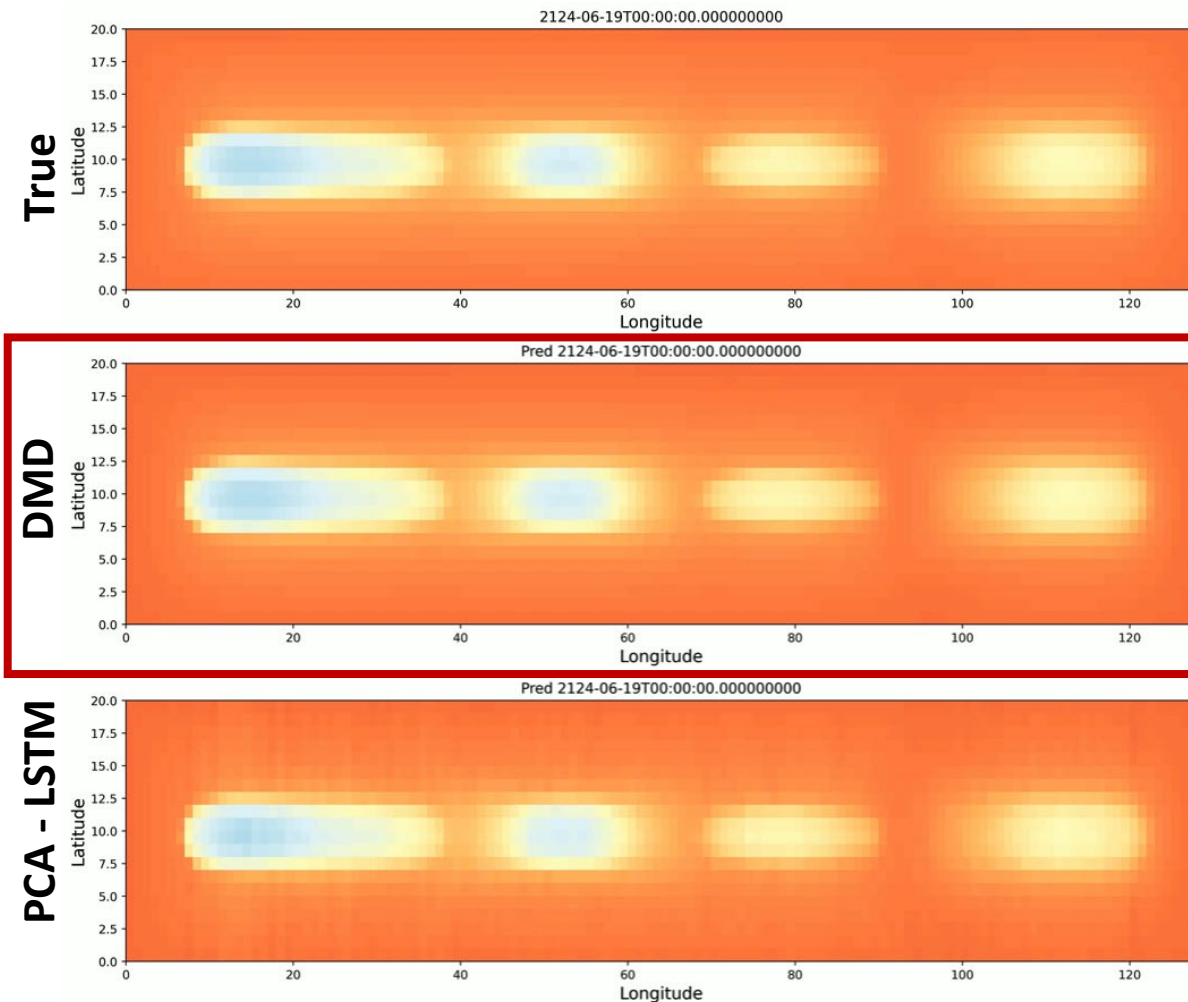
- Compared with PCA-LSTM, DMD can fit well both in peak region and smooth region.
- DMD** has the **best prediction** accuracy and stability among other models in ROM.



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# Summary



## Summary

Perform time, space, frequency and modes analysis of systems.

Based on PCA reduce the system's order and apply three main-stream models to predict system status. (**PCA-LSTM best**)

Apply DMD-Koopman to predict the system and compare with PCA-LSTM. (**DMD-Koopman better**)





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# Thanks for listening!

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